

DEFENSE OF THE DOCTORAL DISSERTATION

DEPARTMENT OF MATHEMATICS

“Cross Effects and Stability”

Bridget Schreiner



Thursday, June 27, 2024

Time: 4:00 PM

Zoom URL: notredame.zoom.us/j/3082757627



Examination Committee:

Mark Behrens, Advisor

Pavel Mnev

Andy Putman

Larry Taylor



Abstract:

We consider a generalization of the cross effects of Eilenberg and Mac Lane to categories suitable for studying homological and representation stability. Specifically, we consider functors $C \rightarrow \mathcal{T} \text{ op}^*$ where C is \mathbf{N} or \mathbf{FI} , the category of finite sets and injections. We construct a spectral sequence computing the homology of our cross effects from the homology of such functors, as well as a spectral sequence reconstructing the homology of the values of the functor from the homology of its cross effects. Finally, we consider these cross effects in the context of the mod 2 homology of the symmetric groups.