# **Department of Mathematics**University of Notre Dame

## **LOGIC SEMINAR**

**Guest Speaker: James Walsh** 

**Cornell University** 

Date: Tuesday, February 7, 2023

**Time:** 2:00 PM

Location: 125 Hayes-Healy Hall

**Zoom URL:** NA



### Lecture Title:

## New results on incompleteness and ordinal analysis

#### Abstract

We present an analogue of Gödel's second incompleteness theorem. Whereas Gödel showed that sufficiently strong theories that are  $\Pi_1^0$ -sound and  $\Sigma_1^0$ -definable do not prove their own  $\Pi_1^0$ -soundness, we prove that sufficiently strong theories that are  $\Pi_1^1$ -sound and  $\Sigma_1^1$ -definable do not prove their own  $\Pi_1^1$ -soundness. Our proof does not involve the construction of a self-referential sentence but rather relies on ordinal analysis. We then turn to characterizations of ordinal analysis itself. One of the main goals of ordinal analysis is measuring the "strength" of theories by calculating their proof-theoretic ordinals. But in what sense do proof-theoretic ordinals measure the strength of theories? What is the attendant notion of strength? We provide some abstract answers to this question.