

## ***TOPOLOGY SEMINAR***

**Guest Speaker: Lvzhou Chen**  
**Purdue University**

**Date:** Tuesday, November 29, 2022

**Time:** 2:15 PM

**Location:** 117 Hayes-Healy Hall

**Zoom Link:** NA

***Lecture Title:***

**The Kervaire conjecture and the minimal complexity of surfaces**



***Abstract***

We use topological methods to solve special cases of a fundamental problem in group theory, the Kervaire conjecture, which has connection to various problems in topology. The conjecture asserts that, for any nontrivial group  $G$  and any element  $w$  in the free product  $G * Z$ , the quotient  $(G * Z) / \langle\langle w \rangle\rangle$  is still nontrivial. We interpret this as a problem of estimating the minimal complexity (in terms of Euler characteristic) of surface maps to certain spaces. This gives a conceptually simple proof of Klyachko's theorem that confirms the Kervaire conjecture for any  $G$  torsion-free. We also obtain new results concerning injectivity of the map  $G \rightarrow (G * Z) / \langle\langle w \rangle\rangle$  when  $w$  is a proper power.