

# ***ALGEBRAIC GEOMETRY AND COMMUTATIVE ALGEBRA SEMINAR***

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**Date:** Tuesday, March 22, 2022

**Time:** 2:30 PM

**Location:** 258 Hurley Hall

**Zoom URL:** NA



**Lecture Title:**

**Rank 3 quadratic generation of Veronese varieties**

**Abstract**

Let  $X$  be any nondegenerate projective variety over an algebraically closed field  $K$  with  $\text{char}(K) \neq 2$  and  $L$  be any very ample line bundle on  $X$ . We say that  $(X, L)$  satisfies property  $QR(k)$  if the homogeneous ideal of  $X \subset \mathbb{P}H^0(X, L)$  can be generated by quadrics of rank at most  $k$ . It is well-known that many classical varieties such as any Segre-Veronese embeddings, rational normal scrolls and curves of high degree satisfy  $QR(4)$ . In this talk, we consider rank 3 quadratic generation for Veronese varieties. We first introduce some methods to produce rank 3 quadrics and explain how to prove any Veronese variety  $\nu_d(\mathbb{P}^n)$  satisfies  $QR(3)$  by applying these methods. We also show some generalization of it to any variety under some positive embedding. Some families of examples with  $QR(k)$  for low  $k$  will be presented in the talk as well.