

## ***GEOMETRIC ANALYSIS SEMINAR***

**Speaker: Renato Bettiol**  
**Lehman College, CUNY**

**Date:** Thursday, March 18, 2021

**Time:** 11:00 AM

**Location:** Zoom

**Zoom URL:** [notredame.zoom.us/j/96288130964?pwd=c2dDelJJTXhSdTBVSEtLYlI1NEdzZz09](https://notredame.zoom.us/j/96288130964?pwd=c2dDelJJTXhSdTBVSEtLYlI1NEdzZz09)



**Lecture Title:**  
**Geography of pinched 4-manifolds**

***Abstract***

It is widely expected that a simply connected closed 4-dimensional Riemannian manifold with positive sectional curvature must be homeomorphic to the 4-sphere or the complex projective plane. Using a new take on classical techniques, we prove this to be the case if  $M$  is  $\delta$ -pinched with  $\delta = \frac{1}{1+3\sqrt{3}} \cong 0.161$ , that is, if all sectional curvatures of  $M$  lie in the interval  $[\delta, 1]$ . We also give new restrictions on the “geography problem” for 4-manifolds under any (positive or negative) pinching assumption. The main tools used are convex algebro-geometric and optimization insights on sets of pinched curvature operators. This is based on joint work with M. Kummer and R. Mendes.