Department of Mathematics University of Notre Dame

TOPOLOGY SEMINAR

Guest Speaker: Aravind Asok University of Southern California

Date: Tuesday, October 27, 2020 Time: 2:30 PM Location: Zoom Zoom Link: https://notredame.zoom.us/j/97262637721

Lecture Title: Algebraic vs. topological vector bundles

Abstract

Suppose X is your favorite (smooth) complex algebraic variety. When does a complex vector bundle on the complex manifold defined by X admit an algebraic structure? This is a long-studied question with close links to various classical questions in the cohomology of algebraic varieties. I will explain how when X is affine, this problem can be reformulated in entirely (motivic) homotopy theoretic terms, and discuss an approach to analyzing this question for arbitrary X. In particular, I will discuss some results obtained jointly with Jean Fasel and Mike Hopkins about algebraic vector bundles on low-dimensional smooth projective varieties and projective space (not necessarily low dimensional).

