

# ***ALGEBRAIC GEOMETRY AND COMMUTATIVE ALGEBRA SEMINAR***

**Speaker: Juan Migliore**  
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**Date:** Wednesday, January 29, 2020

**Time:** 3:00 PM

**Location:** 258 Hurley Hall

***Lecture Title:***

**The singular locus of a hyperplane arrangement in  $P^3$ , and liaison**

***Abstract***

This talk will describe joint work with Uwe Nagel and Hal Schenck. Let  $A$  be a hyperplane arrangement in  $P^3$ . (Much of the work actually holds in  $P^n$ .) Let  $J$  be the Jacobian ideal of  $A$ . This ideal is usually not unmixed, or even saturated. We consider two associated ideals,  $J^{\text{top}}$  and  $\sqrt{J}$ , both of which ARE unmixed and define equidimensional curves  $X^{\text{top}}$  and  $X^{\text{red}}$  in  $P^3$ . These curves both have a claim to being called the (unmixed) singular locus of  $A$ . If a certain fairly mild combinatorial property (\*) of the incidence lattice of  $A$  is satisfied, both  $X^{\text{top}}$  and  $X^{\text{red}}$  are arithmetically Cohen-Macaulay (ACM). If (\*) does not hold, either or both of these curves may fail to be ACM. In fact, they can be made to fail to be ACM by as much as you like (as measured by the dimension of the Hartshorne-Rao module). The proofs use tricks from liaison, which in turn prompt liaison-related questions. We will briefly review facts from liaison along the way.